Code: BA1T5

I MBA-I Semester-Regular Examinations FEBRUARY 2014

QUANTITATIVE TECHNIQUES FOR BUSINESS DECISIONS

Duration: 3hours Max. Marks: 70

SECTION-A

1. Answer any FIVE of the following:

 $5 \times 2 = 10 M$

- a) The student body of a large university consists of 60% female students. A random sample of 8 students is selected. What is the probability that among the students in the sample at least 7 are female?
- b) The average number of calls received by a switchboard in a 30-minute period is 15. What is the probability that between 10:00 and 10:30 the switchboard will receive fewer than 7 calls?
- c) Describe briefly the least cost method to find the initial basic feasible solution of transportation problem
- d) For a Binomial Distribution, p = 0.6 and n = 8, Find P(r < 3).
- e) Explain briefly if there is any relationship between type-I error and the level of significance?
- f) Define i) feasible solution and
 - ii) optimal solution.
- g) Briefly explain Hungarian assignment method.

SECTION - B

Answer the following:

 $5 \times 10 = 50 M$

2. a) For what values of k the equations x + y + z = 1, 2x + y + 4z = k, $4x + y + 10z = k^2$ have a solution and solve them completely in each case.

OR

b) Find the frequency table, calculate median and mode:

Daily Exp (Rs)	0-10	10-20	20-30	30-40	40-50	50-60
No. of families	12	18	30	20	15	5

- 3. a) According to Bureau of labour statistics, the average weekly pay for a production worker was \$441.50. Assume that available data indicate the production worker wages are normally distributed with a standard deviation of \$90.
 - i) What is the probability that a worker earned more than \$400.
 - ii) How much did the production worker have to earn to be in the top 20% of wage earned?
 - iii) What is the probability that a worker earned less than \$300.
 - b) Because refunds are paid more quickly on tax returns that are filed electronically, the Commissioner of the internal revenue service was wondering whether refunds due on returns filed by mail were smaller than those due on returns filed electronically. Looking only at returns claiming refunds, a sample of 17 filed by mail had an average refund of \$563 and a standard deviation of \$378. The average refund on a sample of 13 electronically filed returns was \$958 and the sample standard deviation was \$619. At a significance level of 0.01, do these data support the Commissioner's speculation?

4. a) A GMAC MBA new- matriculant's survey provided the following data for 2018 students.

	Applied to more than 1 school			
		Yes	No	
1	23 and under	207	201	
Age Group	24-26	299	379	
	27-30	185	268	
	34-35	66	193	
	36 and over	51	169	

i) For a randomly selected MBA student, prepare a joint probability table for the experiment consisting of observing the students age and whether the student applied to one or more schools.

ii) What is the probability that a randomly selected applicant is 23 or under?

OR

b) Seagate Foods, Inc., is redesigning the checkout lanes in its supermarkets throughout the country and is considering two designs. Tests on customer checkout times conducted at two stores where the two new systems have been installed result in the following summary of the data.

System A
$$n_1 = 100$$
System B
 $n_2 = 80$ $\overline{x}_1 = 4.1 \text{ min}$ $\overline{x}_2 = 3.4 \text{min}$ $\sigma_1 = 2.2 \text{ min}$ $\sigma_2 = 1.5 \text{min}$

Test at the 0.05 level of significance to determine whether the populations mean checkout times of the two systems differ.

5. a) Solve the following LPP:

Maximise
$$Z=20X_1+30X_2$$
; Subject to $4X_1+3X_2 \le 40$; $2X_1+5X_2 \le 28$; $8X_1+2X_2 \le 36$ and X_1 , $X_2 \ge 0$. OR

b) A departmental head has four subordinates and four tasks to be performed. The subordinates differ in efficiency and the tasks differ intrinsic difficulty. His estimates of the times that each man would take to perform each task are given below in matrix:

		Ta	asks	•		
Subordinate	I	II	Ш	IV		
A	8	26	17	11		
\mathbf{B}	13	28	4	26		
\mathbf{C}	38	19	18	15		
D	19	26	24	10		

Find the optimal assignments of tasks to subordinates so that the time is minimum.

6. a) A company has three factories at Amethi, Baghpat and Gwalior having production capacity of 5000, 6000 and 2500 tonnes

respectively. Four distribution centres at Allahabad, Bombay, Calcutta and Delhi requiring 6000 tonnes, 4000 tonnes, 2000 tonnes and 1500 tonnes respectively of the product. The transportation costs per tonne from different factories to different centers are given below:

Factories		Distribution Cente	ers	
	Allahabad	Bombay	Calcutta	Delhi
Amethi	3	2	7	6
Baghpat	7	5	2	3
Gwalior	2	5	4	5

Find the transportation cost and the schedule of transportation.

OR

b) Find the optimal strategies for A and B in the following game. Also obtain the value of the game.

		B's strategy		
		$\mathbf{b_1}$	$\mathbf{b_2}$	$\mathbf{b_3}$
	$\mathbf{a_1}$	9	8	-7
A's strategy	$\mathbf{a_2}$	3	-6	4
	a ₃	6	7	-7

SECTION - C

7. Case Study

 $1 \times 10 = 10 M$

A television co. has three major departments to manufacture two of it's models A & B. The monthly capacities are given as follows:

	Per Unit time	e requirement	Hours available	
	Model A	Model B	this month	
Department I	4.0	2.0	1600	
Department II	2.5	1.0	1200	
Department III	4.5	1.5	1600	

The marginal profit per unit from model A is Rs. 400 & that of model B is Rs.100. Assume that the company can sell any quantity of either product due to favorable market conditions. Formulate this as a linear programming problem and solve by graphic method for optimum output for both the models, the highest possible profit for this month & the slack time in the three departments.